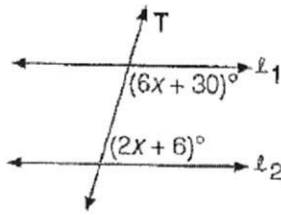


1. What is the value of x that makes $\ell_1 \parallel \ell_2$?



$$6x + 30 + 2x + 6 = 180$$

$$8x + 36 = 180$$

$$\underline{-36 \quad -36}$$

$$\frac{8x}{8} = \frac{144}{8}$$

$$x = 18$$

D) 6

A) 18

B) -6

C) 12

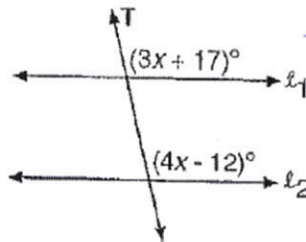
2. What is the value of x that makes $\ell_1 \parallel \ell_2$?

$$3x + 17 = 4x - 12$$

$$3x + 17 = 4x - 12$$

$$\underline{-3x \quad +12 \quad -3x \quad +12}$$

$$29 = x$$



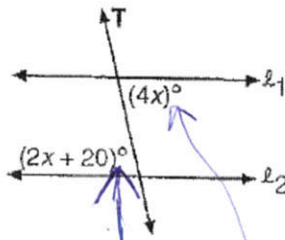
D) 25

A) 5

B) 29

C) 26.4

3. What is the value of x that makes $\ell_1 \parallel \ell_2$?



$$4x = 2x + 20$$

$$4x = 2x + 20$$

$$\underline{-2x \quad -2x}$$

$$2x = 20$$

$$x = 10$$

D) 26.6

A) 11.6

B) 10

C) 8

4. Two parallel lines are cut by a transversal. The measures of two alternate interior angles are represented by $4x$ and $2x + 20$. Find the value of x .



5. Two parallel lines are cut by a transversal. The measures of two interior angles on the same side of the transversal are represented by $3x - 12$ and $5x + 32$. Find the value of x .

$$3x - 12 + 5x + 32 = 180$$

$$8x + 20 = 180$$

$$\underline{-20 \quad -20}$$

$$8x = 160$$

$$x = 20$$

are supplementary

6. Two parallel lines are cut by a transversal. The measures of two corresponding angles are represented by $4x - 6$ and $2x + 12$. Find the value of x .

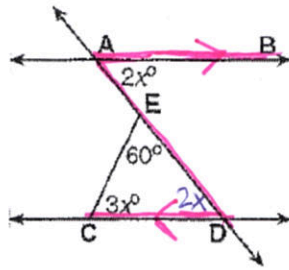
$$4x - 6 = 2x + 12$$

$$\underline{-2x \quad +6 \quad -2x \quad +6}$$

$$2x = 18$$

$$x = 9$$

7. In the accompanying diagram, \overline{AB} is parallel to \overline{CD} , \overline{AED} is a transversal, and \overline{CE} is drawn.



If $m\angle CED = 60^\circ$, $m\angle DAB = 2x^\circ$, and $m\angle DCE = 3x^\circ$, find x .

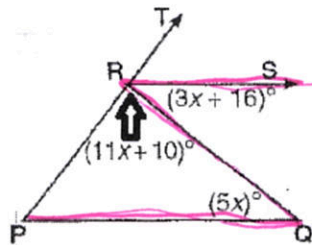
$$60 + 3x + 2x = 180$$

$$-60 \qquad -60$$

$$\frac{5x}{5} = \frac{120}{5}$$

$$x = 24$$

8. In the figure below, $\overline{RS} \parallel \overline{PQ}$.



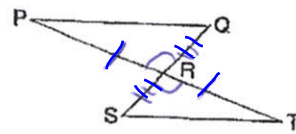
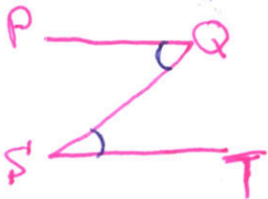
$$3x + 16 = 5x$$

$$-3x \qquad -3x$$

$$\frac{16}{2} = \frac{2x}{2}$$

$$x = 8$$

Find the $m\angle PRQ = 11(8) + 10 = 98$



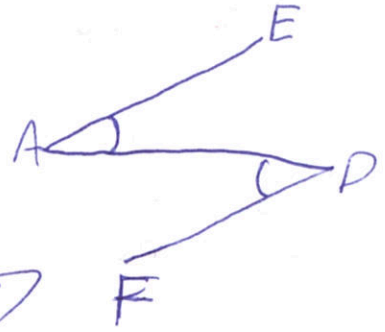
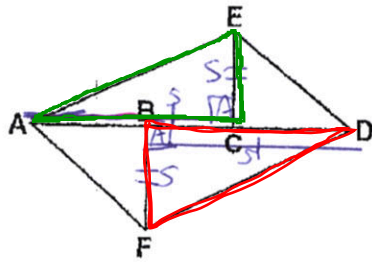
Given: \overline{PT} and \overline{QS} bisect each other

Prove: $\overline{PQ} \parallel \overline{ST}$

- S [① \overline{PT} and \overline{QS} bisect each other
- ② $\overline{PR} \cong \overline{RT}$
- A [③ \overline{PT} and \overline{SQ} intersect at R
- ④ $\angle PRQ \cong \angle SRT$
- S [⑤ $\overline{SR} \cong \overline{RQ}$
- ⑥ $\triangle PRQ \cong \triangle SRT$
- ⑦ $\angle PQR \cong \angle RST$
- ⑧ $\overline{PQ} \parallel \overline{ST}$

- ① Given
- ② bisector cuts segment into 2 \cong halves
- ③ Given
- ④ intersecting lines create \cong vertical \angle 's
- ⑤ step 2
- ⑥ SAS \cong SAS
- ⑦ CPCTC
- ⑧ alt int \angle 's create \parallel lines

10



Given: $\overline{EC} \perp \overline{AD}$
 $\overline{FB} \perp \overline{AD}$
 $BF \cong CE$
 $AC \cong BD$

Prove: $\overline{AE} \parallel \overline{FD}$

S

R

S [1] $AC \cong BD$

[1] Given

A [2] $EC \perp AD, FB \perp AD$

[2] Given

A [3] $\angle ACE$ and $\angle DBF$ are
 Rt \angle 's

[3] \perp lines form Rt \angle 's

[4] $\angle ACE \cong \angle DBF$

[4] All Rt \angle 's \cong

S [5] $BF \cong CE$

[5] Given

[6] $\triangle ACE \cong \triangle BFD$

[6] SAS \cong SAS

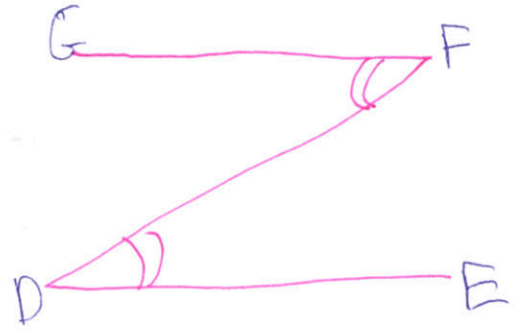
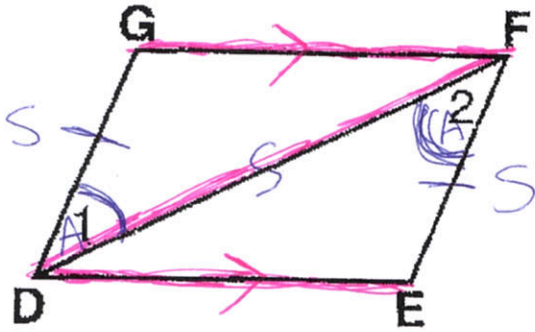
[7] $\angle EAC \cong \angle BDF$

[7] CPCTC

[8] $AE \parallel FD$

[8] alt int \angle 's form \parallel lines

(11)



Given: $\angle 1 \cong \angle 2$
 $\overline{DG} \cong \overline{FE}$

Prove: $GF \parallel DE$

S

R

S [(1) $\overline{DG} \cong \overline{FE}$

(1) Given

A [(2) $\angle 1 \cong \angle 2$

(2) Given

S [(3) $\overline{DF} \cong \overline{DF}$

(3) Reflexive

(4) $\triangle DGF \cong \triangle DFE$

(4) SAS \cong SAS

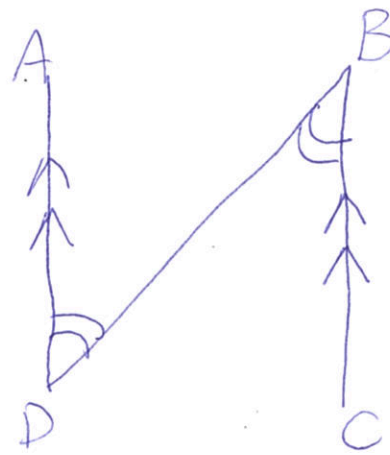
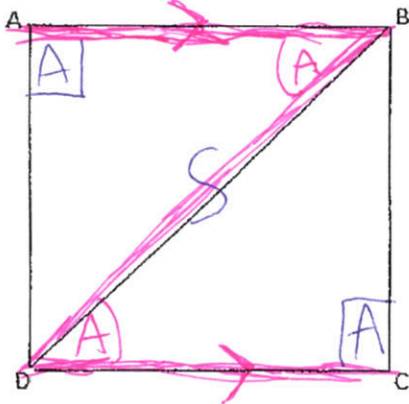
* (5) $\angle GFD \cong \angle FDE$

(5) CPCTC

(6) $GF \parallel DE$

(6) alt int \angle s create \parallel lines

121



CPCTC'S

Given: $AB \parallel DC$
 $AD \perp AB$
 $CD \perp BC$

Prove: $AD \parallel BC$

S

R

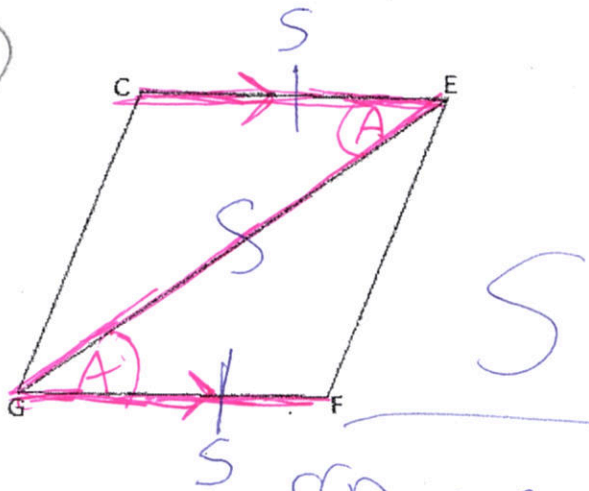
- A
- ① $AD \perp AB, CD \perp BC$
 - ② $\angle BAD$ and $\angle BCD$ are Rt \angle s
 - ③ $\angle BAD \cong \angle BCD$

- A
- ④ $AB \parallel DC$
 - ⑤ $\angle ABD \cong \angle BDC$

- S
- ⑥ $BD \cong BD$
 - ⑦ $\triangle ABD \cong \triangle BCD$
 - * ⑧ $\angle ADB \cong \angle DBC$
 - ⑨ $AD \parallel BC$

- ① Given
- ② \perp lines form Rt \angle s
- ③ all Rt \angle s \cong
- ④ Given
- ⑤ \parallel lines form \cong alt int \angle s
- ⑥ Reflexive
- ⑦ $AAS \cong AAS$
- ⑧ CPCTC
- ⑨ alt int \angle s form \parallel lines

15.



Given: $\overline{CE} \parallel \overline{GF}$
 $\overline{CE} \cong \overline{GF}$

Prove: $\overline{GC} \cong \overline{FE}$

S [1] $\overline{CE} \cong \overline{GF}$

A [2] $\overline{CE} \parallel \overline{GF}$
 [3] $\angle CEG \cong \angle FGE$

S [4] $\overline{GE} \cong \overline{GE}$

[5] $\triangle GCE \cong \triangle GEF$

[6] $\overline{GC} \cong \overline{FE}$

[1] Given

[2] Given

[3] // lines for \cong
alt int \angle 's

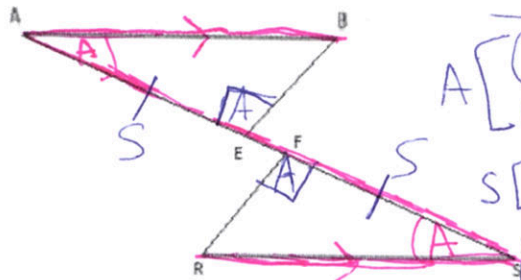
[4] Reflexive

[5] SAS \cong SAS

[6] CPCTC

R

16.



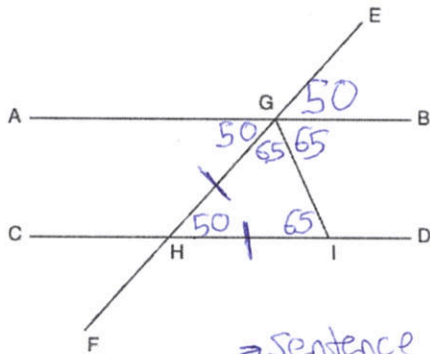
Given: $AB \parallel RS$
 $BE \perp AF$
 $RF \perp ES$
 $\overline{AE} \cong \overline{FS}$

Prove: $\angle B \cong \angle R$

- A [(1) $AB \parallel RS$
 (2) $\angle BAE \cong \angle SFR$
 S [(3) $AE \cong FS$
 (4) $BE \perp AF, RF \perp ES$
 A (5) $\angle BEA$ and $\angle SFR$
 are $Rt \angle$'s
 (6) $\angle BEA \cong \angle SFR$
 (7) $\triangle BAE \cong \triangle SFR$
 (8) $\angle B \cong \angle R$

- S (1) Given
 (2) \parallel lines for \cong alt int \angle 's
 (3) Given
 (4) Given
 (5) \perp lines form $Rt \angle$'s
 (6) all $Rt \angle$'s \cong
 (7) $ASA \cong ASA$
 (8) CPCTC

17. In the diagram below, \overline{EF} intersects \overline{AB} and \overline{CD} at G and H , respectively, and \overline{GI} is drawn such that $\overline{GH} \cong \overline{IH}$.



If $m\angle EGB = 50^\circ$ and $m\angle DIG = 115^\circ$, explain why $\overline{AB} \parallel \overline{CD}$.

$$50 + x + x = 180$$

$$2x = 130$$

$$x = 65$$

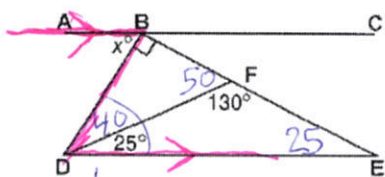
Since the alt int \angle 's are \cong ,
 the \parallel lines are formed

18. In the accompanying diagram, $\overline{ABC} \parallel \overline{DE}$, $m\angle FDE = 25^\circ$, $m\angle DFE = 130^\circ$, and $m\angle ABD = x^\circ$.

$$90 + 50 + m = 180$$

$$140 + m = 180$$

$$m = 40$$



$$25 + 130 + y = 180$$

$$155 + y = 180$$

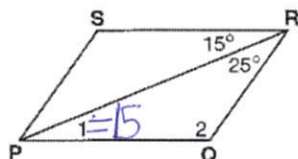
$$-155 \quad -155$$

$$y = 25$$

What is the value of x ?

$$40 + 25 = x$$

19. If $\overline{PQ} \parallel \overline{SR}$ and $\overline{PS} \parallel \overline{QR}$, find $m\angle 1$ and $m\angle 2$.



$$25 + 15 + (\angle 2) = 180$$

$$40 + x = 180$$

$$\angle 2 = 140$$