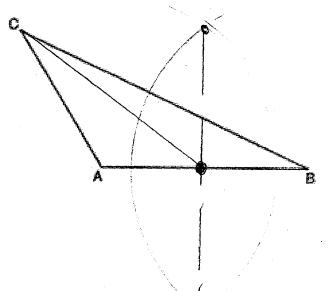
# **Geometry Pre-IB Mid-term Review**

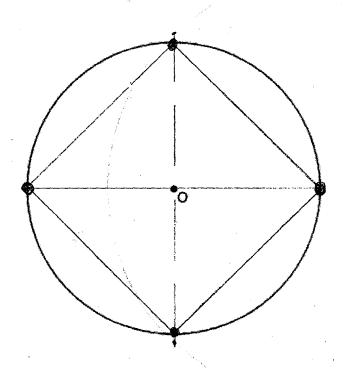
# Constructions

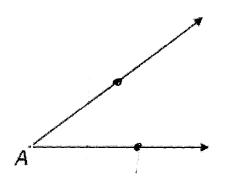
In the diagram of  $\triangle ABC$  shown below, use a compass and straightedge to construct the median to  $\overline{AB}$ . [Leave all construction marks.]

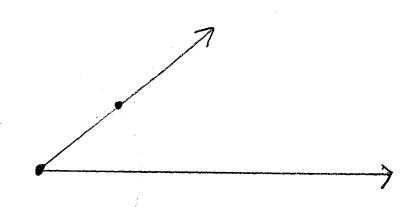


Using a straightedge and compass, construct a square inscribed in circle O below.

[Leave all construction marks.]







4.

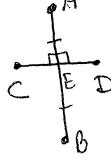
(1) 
$$\overline{AD}$$
,  $\overline{BD}$ 

(2) 
$$\overline{AC}$$
,  $\overline{BC}$ 

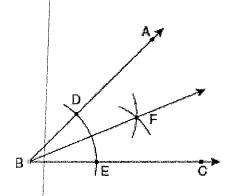
Segment 
$$CD$$
 is the perpendicular bisector of  $\overline{AB}$  at  $E$ . Which pair of segments does not have to be a nigrount?

$$AE, \overline{BE}$$

$$(1)$$
  $\overline{DE}$ ,  $\overline{CE}$ 



5)The diagram below shows the construct -n of the bisector of  $\angle ABC$ .



Which statement is not true?

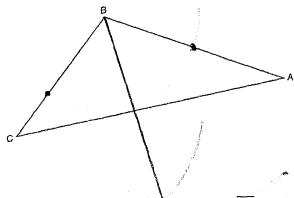
1) 
$$\mathbf{m} \angle EBF = \frac{1}{2} \mathbf{m} \angle ABC$$

2) 
$$\mathbf{m} \angle DBF = \frac{1}{2} \mathbf{m} \angle ABC$$

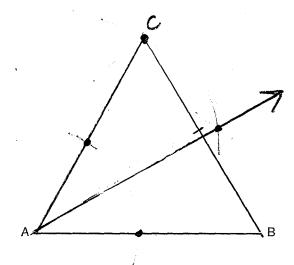
$$(3)$$
 m $\angle EBF = m\angle ABC$ 

4) 
$$\mathbf{m} \angle DBF = \mathbf{m} \angle EBF$$

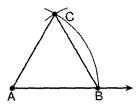
6)Using a compass and straightedge, construct the bisector of  $\angle CBA$ . [Leave all construction marks.]



7)Using a compass and straightedge, construct an equilateral triangle with  $\overline{AB}$  as a side. Using this triangle, construct a 30° angle with its vertex at A. [Leave all construction marks.]



8) The diagram below shows the construction of an equilateral triangle.



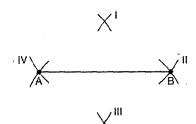
Which statement justifies this construction?

1) 
$$\angle A + \angle B + \angle C = 180$$

2) 
$$\mathbf{m} \angle A = \mathbf{m} \angle B = \mathbf{m} \angle C$$

4) 
$$AB + BC > AC$$

9)Line segment AB is shown in the diagram How.



Which two sets of construction marks, labe d, II, III, and IV, are part of the construction of the perpendicular bisector of line segment AB?

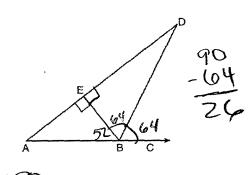
- 1) land II
- (2) I and III
  - 3) II ard III
  - 4) II arıd IV

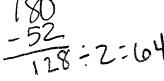
# Theorems and Vocabulary and Properties int/ext angle, sum of int angles of triangle, isosceles triangle)

10)When writing a geometric proof, which ingle relationship could be used alone to justify that two angles are congruent?

- 1) supplementary angles
- 2) linear pair of angles

- 3) adjacent angles
- 4) vertical angles
- 11) The diagram below shows  $\triangle ABD$ , wit  $\overrightarrow{ABC}$ ,  $\overrightarrow{BE} \perp \overrightarrow{AD}$ , and  $\angle EBD \cong \angle CBD$ . If  $\mathbf{m} \angle ABE = 52$ , what is:  $\angle D$ ?
- **1)** 26
  - 2) 38
  - 3) 52
  - 4) 64,





# 36 54 90

12) Triangle PQR has angles in the ratio of 2:3:5. Which type of triangle is  $\triangle PQR$ ?

1) acute

2) isosceles

x = 18

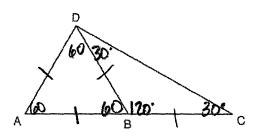
3) obtuse

(4) right

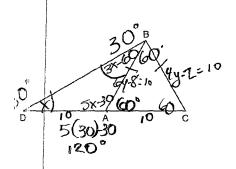
13)In  $\triangle ABC$ , the measure of angle A is fifteen less than twice the measure of angle B. The measure of angle C equals the sum of the measures of angle A and angle B. Determine the measure of angle B.

$$X + 2x - 15 + (x + 2x - 15) = 180$$
  
 $(0x - 30 = 180)$   
 $(6x = 210)$   
 $(x = 35) = maB$ 

14)In the diagram below of  $\triangle ACD$ , B is a point on AC such that  $\triangle ADB$  is an equilateral triangle, and  $\triangle DBC$  is an isosceles triangle with  $\overline{DB} \cong \overline{BC}$ . Find  $\mathbf{m} \angle C$ . Explain your reasoning.

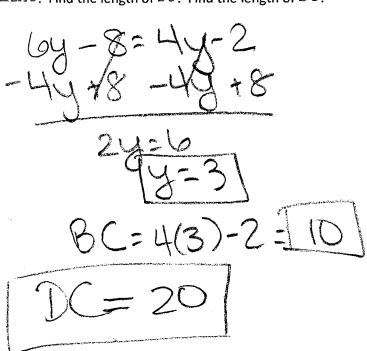


M4C=30

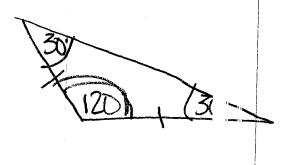


In  $\triangle DAB$ ,  $m\angle D=x$ ,  $m\angle DAB=5x-30$ , and  $m\angle DBA=3x-60$ . In  $\triangle ABC$ , AB=6y-8 and BC=4y-2. [Only algebraic solutions can receive full credit.] Find  $m\angle BAC$ . Find the length of  $\overline{BC}$ . Find the length of  $\overline{DC}$ .

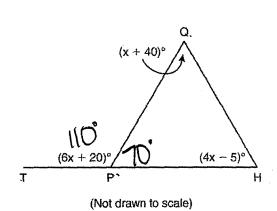
9x-90=180 9x=270 x=30 m=30 m > BAC=60



16) Hersch says if a triangle is an obtuse tarrow then it cannot also be an isosceles triangle. Using a diagram, show that Hersch is incorrect, and indicate the measures of all the angles to justify your answer.



17)In the diagram below of  $\triangle HQP$ , side HP is extended through P to T,  $m\angle QPT = 6x + 20$ ,  $m\angle HQP = x + 40$ , and  $m\angle PHQ = 4x - 5$ . Find  $m\angle QPT$ .



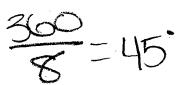
$$0x+20 = x+40+4x-5$$
  
 $0x+20 = 5x+35$   
 $-5x-20 - 3x - 20$   
 $x=15$ 

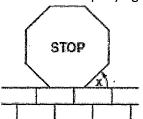
18)A stop sign in the shape of a regular octagon is resting on a brick wall, as shown in the accompanying diagram.

What is the measure of angle x?

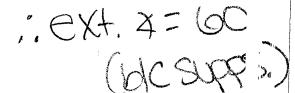


- 2) 60°
- 3) 120°
- 4) 135°





19)The measure of an interior angle of a regular polygon is 120°. How many sides does the polygon have?



20)The sum of the interior angles of a regue polygon is 540°. Determine and state the number of degrees in one interior angle of the polygon.

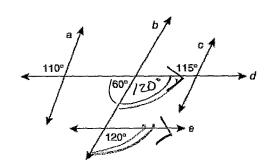
$$180(0-2) = 510$$
 $180(0-2) = 510$ 
 $180$ 
 $180$ 
 $180$ 
 $180$ 
 $180$ 
 $180$ 
 $180$ 

# **Parallel Lines**

21)Based on the diagram below, which stall ment is true?

- 1) a | b
- 2) a || a
- 3) b | c





If  $\mathbf{m} \angle 1 = 7x - 36$  and  $\mathbf{m} \angle 2 = 5x + 12$ , for which value of x would  $p \parallel q$ ?



- 2) 24
- 3) 83
- 4) 97

$$7x-36+5x+12=180$$

$$12x-24=180$$

$$+24=124$$

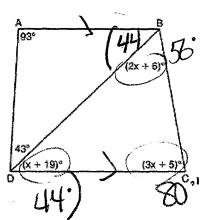
$$12x=204$$

$$x-17$$

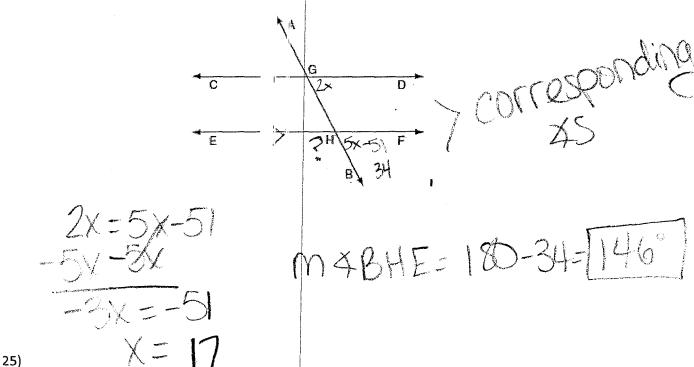
In the diagram below of quadrilateral ABCD with diagonal  $\overline{BD}$ ,  $m\angle A = 93$ ,  $m\angle ADB = 43$ ,  $m\angle C = 3x + 5$ ,  $m\angle BDC = x + 19$ , and  $m\angle DBC = 2x + 6$ . Determine if  $\overline{AB}$  is parallel to  $\overline{DC}$ . Explain your reasoning.

180 - 43 - 43

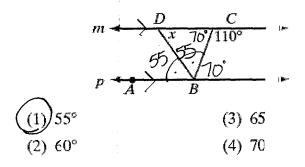
23)



YOS, FOILDC blc the att. 17. 20 of 4ABD + 4CDB are both = to U4" (:=)



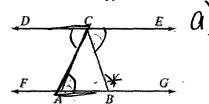
In the figure given, lines m and p are parallel and  $\overline{BD}$  bisects  $\angle ABC$ . What is the measure if  $\angle x$ ?



Given:  $\angle CAB \cong \angle DCA$  and  $\angle DCA \cong \angle ECB$ 

Prove: a. AB | DCE.

**b.**  $\angle CAB$  is the supplement of  $\angle CBG$ .



a) 2. AB 11 SCE

3. 4 ECB is a supp. to 4CBG

4. MXECB+MACBG

1. given

2 lines are a transversal = aut. int. xs. the lines are 11.

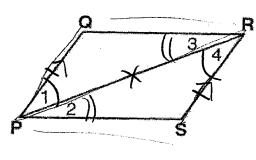
lines Cut 649 side int. 45 that are supplementary 4. SUPP! AS add of

5. transitive prop.

27)

Given:  $\overline{QP} \parallel \overline{RS}, \overline{QP} \cong \overline{RS}$ 

Prove:  $\overline{QR} \parallel \overline{PS}$ 



6. macaben acos

I. OPLIES OPERS

2. 41 = 44

3. PR = PR

4. DOPR= DSRP

5. 42° ×3

6 ORIL PS

Given

3. reflexive prop.

SAS SA

### **Rotations**

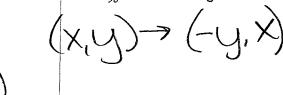
28)What is the image of point (8,-4) under the rotation  $R_{90}$  about the origin?

1) (8,4)



3) (-4,8)

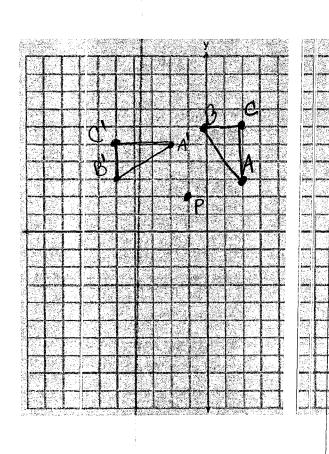
4) (-4, -8)



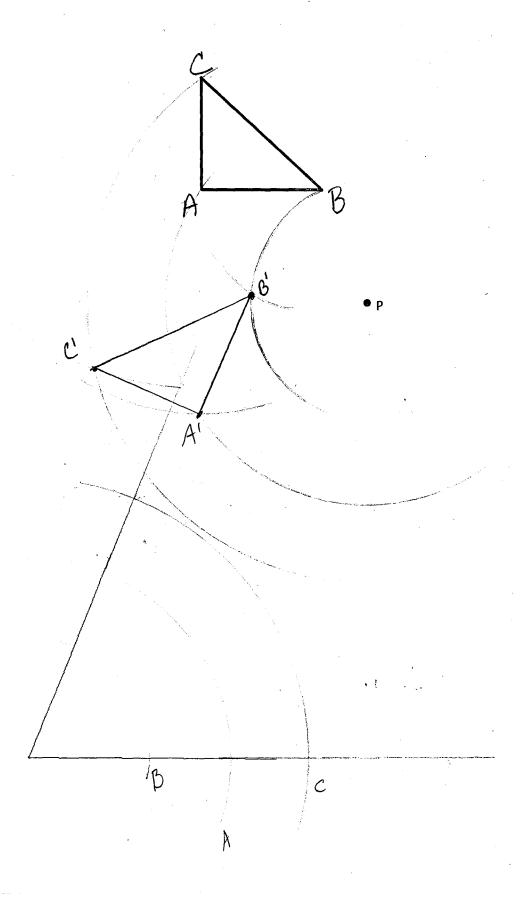
29)

Given  $\triangle ABC$  with vertices A(2,3 B(0,6)) and C(2,6).

- a. Graph  $\triangle ABC$  on the axes | ovided below.
- b. Graph and state the coord ates of  $\Delta A'B'C'$ , the image of  $\Delta ABC$  after a rotation of 90° about the point (-1, 2')



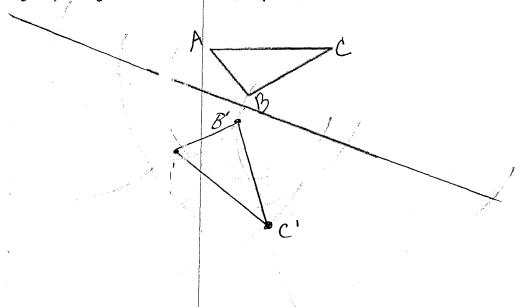
$$(x_{1}y)^{T_{1}-2}(x+1,y-2)$$
 $R_{90}$   $(-(y-2), x+1)$ 
 $(-y+2, x+1)$ 
 $T_{-1}$   $(-y+1, x+3)$ 
 $A': (-3+1, 2+3) = (-2,5)$ 
 $B': (-(b+1, 0+3)) = (-5,3)$ 
 $C': (-(b+1, 2+3)) = (-5,5)$ 



### Reflections

31)

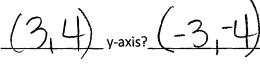
Reflect the given pre-image across the line of reflection provided.



32)What are the coordinates of point P, the image of point (3, -4) after a reflection in the line y = x?

- 1) (3,4)
- 2) (-3,4)
- 3) (4,--3)
- (-4, 3)

Side Note: What would the image be aften reflection in the x-axis?

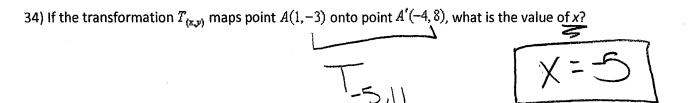


# Translations

33)A translation moves P(3,5) to P'(6,1) . What are the coordinates of the image of point (-3,-5) under the same translation?

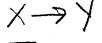
(1) (0,-9)

- 2) (-5,-3)
- 3) (-6,-1)
- 4) (-5,-9)



35)

Point P is on the directed line segment from point X(-6,-2) to point Y(6,7) and divides the segment in the ratio 1:5. What are the =(0.70101)coordinates of point P?



(1) 
$$(4,5\frac{1}{2})$$

(3) 
$$(-4\frac{1}{2},0)$$

(2) 
$$\left(-\frac{1}{2}, -4\right)$$

$$(4)$$
 $(-4,-\frac{1}{2})$ 

+ 2,1,5

# **Composition of Transformations**

36)What is the image that results from this composition of transformations?

 $r_{x-axis} \circ R_{0,90^{\circ}}(-3,0)$ 

$$(-3,0) \rightarrow (0,-3) \rightarrow (0,3)$$

37)The coordinates of  $\triangle JRB$  are J(1,-2), R(-3,6), and B(4,5). What are the coordinates of the vertices of its image after the transformation  $T_{2,-1} \circ r_{y-axis}$ ?

$$J:(1,-2) \rightarrow (-1,-2) \rightarrow (1,-3)$$

$$R: (-3,6)\rightarrow (3,6)\rightarrow (5,5)$$

### **Extra Transformations-**

38) Which transformation is not always a riper motion?

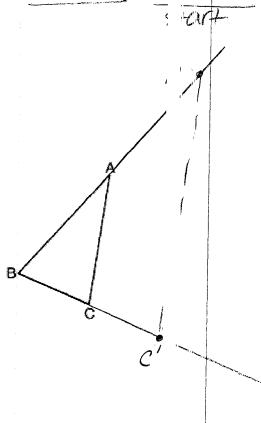
- 1) rotation
- 2) dilation
  - 3) reflection
  - 4) translation

39)A transformation of a polygon that always preserves both length and orientation is

- 1) dilation
- X
- 2) trar slation
  - 3) line reflection 🔀
  - 4) None of the above

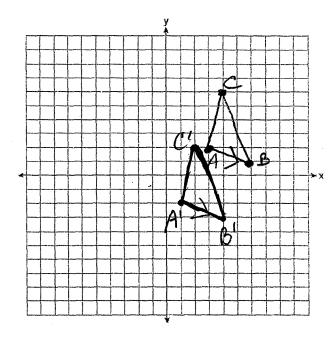
40)

Using a compass and straightedge, instruct and label  $\triangle A'B'C'$ , the image of  $\triangle ABC$  after a dilation with a scale factor of 2 and contered at B. [Leave all construction marks.]



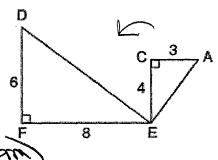
41)The vertices of  $\triangle ABC$  are A(3,2), B(6,1), and C(4,6). Identify and graph a transformation of  $\triangle ABC$  such that its image,  $\triangle A'B'C'$ , results in  $\overline{AB} \parallel \overline{A'B'}$ .

T-2-4



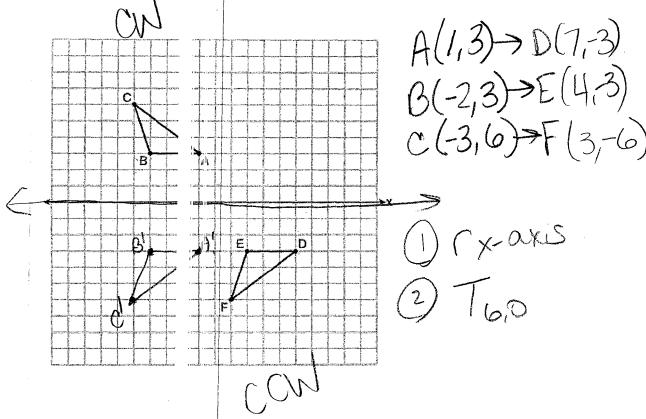
42)

Given:  $\triangle AEC$ ,  $\triangle DEF$ , and  $\overline{FE} \perp \overline{CE}$ 



What is a correct sequence of similarity transformations that shows  $\triangle AEC \sim \triangle DEF$ ?

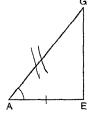
- (1) a rotation of 180 degrees about point E followed by a horizontal translation
- (2) a counterclockwise rotation of 90 degrees about point E followed by a horizontal translation
- (3) a rotation of 180 degrees about point E followed by a dilation with a scale factor of 2 centered at point E
- (4) a counterclockwise rotation of 90 degrees about point E followed by a dilation with a scale factor of 2 centered at point E

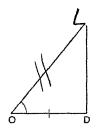


# **Triangle Congruence**

44)In the diagram below of  $\triangle AGE$  and  $\triangle \Box D$ ,  $\angle GAE \cong \angle LOD$ , and  $\overline{AE} \cong \overline{OD}$ .

To prove that  $\triangle AGE$  and  $\triangle OLD$  are con uent by SAS, what other information is needed?



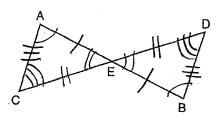


1) 
$$\overline{GE} \cong \overline{LD}$$

$$(2)) \overline{AC!} \cong \overline{OL}$$

3) 
$$\angle A.GE \cong \angle OLD$$

4) 
$$\angle AEG \cong \angle ODL$$



# Which statement is not always true?

1) 
$$\overline{AC} \cong \overline{BD}$$
  $\checkmark$ 

2) 
$$\overline{CE} \cong \overline{DE}$$

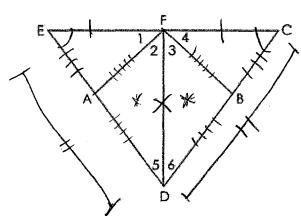
3) 
$$\angle EAC \cong \angle EBD$$

$$(4) \angle ACE \cong \angle DBE \checkmark$$

Prove: △AFD ≅ △BFD

- 3. AFEA \$ AFCB
- 4. AF = BF
- 5. PD = FD
- 6. EA+AD=ED

CB+BD=CD



7. EA+AD=CB/BD

9. DAFDE ABAD

# 1. EFECF, EDECO, 1. GIVEN

2. If 2 sides of

3.SAS=SAS

4. CPCTC

5. reflexive prop.

le partition post.

7. Substitution post

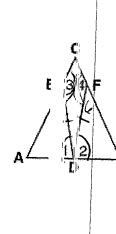
8. subtraction post.

9. SSS = SSS

Given: ∠1 ≃ ∠2

DE = DF ∠3 ≃ ∠4

Prove: AABC is isosceles



1, X1=42, DE=DF, 43=44

inear poirs

3. 43,+x5 and

4. M43+ mx5=180 m44+m36=180°

5. M X 34 M X 5 = M X 4 M 6 6. m 35=mx6

7. DAED = ABPD

8,4A= xB 9. AC= PC

10. AABC is isosceles

1. Giver

2. Ladjacent 45 on a straight line form a linear pair B. If 2 45 torm a linearpair,

are supp.

Supp., their sum is 180°

5. substitution post.

C. Subtraction

7, ASA = ASA

9 TF ZXS, OF a are & the off

SHOS OR & 10. a 1 w 2

= sidos

Prove:  $\overline{XB} \cong \overline{YB}$ 

48)

1. DB L, AC, AB=CB, 41=42 1. Given 2,4081+40BCare 3, ADBA = ADBC 3.all t. ks ares

Given:  $\overline{DB} \perp \overline{AC}; \overline{AB} \cong \overline{CB}; \angle 1 \cong \angle$ 

4 DE S DE 5. 4 DBA = △DR 6. 4A=XC

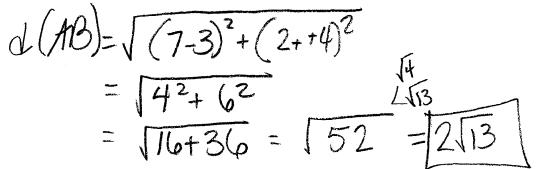
4. Re lexive prop. 5. S 1. S | = SAS

8. XB=YB

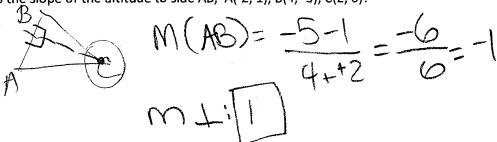
### **Coordinate Geometry**

52)

49) The endpoints of  $\overline{AB}$  are A(3,-4) and B(7,2). Determine and state the length of  $\overline{AB}$  in simplest radical form.



50) What is the slope of the altitude to side AB, A(-2, 1), B(4, -5), C(2, 6)?



51) If a line segment has endpoints A(3x + 5,3y) and B(x - 1,-y), what are the coordinates of the midpoint of  $\overline{AB}$ ?

$$M = \begin{pmatrix} 3X+5+X-1 \\ 2 \end{pmatrix} = \begin{pmatrix} 4X+4 \\ 2 \end{pmatrix} = \begin{pmatrix} 4X+4 \\ 2 \end{pmatrix} = \begin{pmatrix} 21 \\ 2X+2 \end{pmatrix}$$

If the points (3,5), (4,2) and (5,k) lie on a straight line, the value of k is

$$M_1 = \frac{5-2}{3-4} = \frac{3}{-1}$$

$$-3 = K-2$$

$$+2$$

$$+2$$

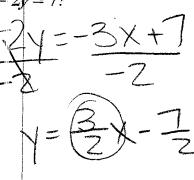
Which equation represents line that is parallel to the line whose equation is (-2y = 7)?

1) 
$$y = -\frac{3}{2}x + 5$$

2) 
$$y = -\frac{2}{3}x + 4$$

$$3) y = \frac{3}{2}x - 5$$

4) 
$$y = \frac{2}{3}x - 4$$



54)

What is the slope of a line that is perpendicular to the line whose equation i 3x + 5y = 4?

1) 
$$-\frac{3}{5}$$

2) 
$$\frac{3}{5}$$

3) 
$$-\frac{5}{3}$$

$$(4) \frac{5}{3}$$

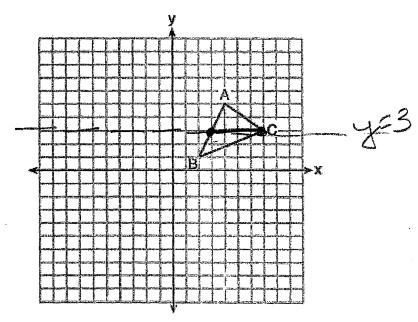
$$51 = -3x + 4$$

55) Which equation represents the perpodicular bisector of AB whose endpoint are A(8,2) and B(0,6)? Express your answer in slope-intercept form.

$$m(AB) = 62 = 4 = -1$$

m1:2

In the diagram below,  $\triangle ABC$  has vertices A(4,5), B(2,1), and C(7,3).



From C(7,3)

Write the equation of the median to side 
$$\underline{AB}$$
.  $M(AB)+(3,3)$ 

$$y-3=0(x-3)$$
  
 $y-3=0$   $y=3$ 

57) A line that passes through the points whose coordinates are (1, 1) and (5, 7) is dilated by a scale factor of 4.

A) Write the equation of the image if the center of dilation is the origin.

 $(1,1) \rightarrow (4,4)$  $(5,7) \rightarrow (20,28)$ 

B) Write the equation of the image if the center of dilation is (5, 7).