

Name: _____

Key

Station Activity

Optimization: Station Activity Date: _____

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| Station # <u>1</u> | We are trying to <u>minimize</u> /maximize <u>surface area</u> . (Circle min or max & fill in the blank) |
| Main equation (this is the equation we are trying to optimize): $S = 2x^2 + 4xh$ | Auxiliary equation (this comes from other information given in the problem): $V = x^2h \rightarrow 200 = x^2h$ |
| Use the auxiliary equation to write your main equation with only two variables: $S = 2x^2 + 4xh$ $S = 2x^2 + 4x\left(\frac{200}{x^2}\right) = 2x^2 + \frac{800}{x} = SA$ | Graph (label axes and sketch a graph): |
| A suitable viewing window to see the min or max: [xmin, xmax] = [0, 10] [ymin, ymax] = [0, 250] | |
| Answer to the original question: <u>min SA = 205.19</u> dimensions: $5.84 \times 5.84 \times 5.86$ | $h = \frac{200}{5.84^2} = 5.86$ |

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| Station # <u>2</u> | We are trying to minimize/ <u>maximize</u> <u>area</u> . (Circle min or max & fill in the blank) |
| Main equation (this is the equation we are trying to optimize): $A = xy$ | Auxiliary equation (this comes from other information given in the problem): $3x + y = 100$ |
| Use the auxiliary equation to write your main equation with only two variables: $A = x(100 - 3x)$ $A = 100x - 3x^2$ | Graph (label axes and sketch a graph): |
| A suitable viewing window to see the min or max: [xmin, xmax] = [0, 36] [ymin, ymax] = [0, 1000] | |
| Answer to the original question: <u>Max area: 833.33 ft²</u> Dimensions: $x = 16.67$ $y = 100 - 3(16.67) = 49.99$ | $y = 100 - 3x$ |

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| Station # <u>3</u> | We are trying to minimize/maximize <u>Volume</u> . (Circle min or max & fill in the blank) | Main equation (this is the equation we are trying to optimize): $V = x^2 h$ |
| Auxiliary equation (this comes from other information given in the problem): $S = x^2 + 4xh$ $70 = x^2 + 4xh$ | Graph (label axes and sketch a graph): | Main equation with only one variable: $\frac{70 - x^2}{4x} = h$ |
| Use the auxiliary equation to write your main equation with only two variables: $V = x^2 h$ $V = x^2 \left(\frac{70 - x^2}{4x} \right) = \frac{70x - x^3}{4}$ | A suitable viewing window to see the min or max: [xmin, xmax] = [0, 10] [ymin, ymax] = [0, 80] | Answer to the original question: Max Volume: <u>56.36 ft³</u> Dimensions: $x = 4.83$ $h = \frac{70 - 4.83^2}{4(4.83)} = 2.42$ |
| Answer to the original question: $4.83 \times 4.83 \times 2.42$ | | Answer to the original question: $4.83 \times 4.83 \times 2.42$ |

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| Station # <u>4</u> | We are trying to minimize/maximize <u>Volume</u> . (Circle min or max & fill in the blank) | Main equation (this is the equation we are trying to optimize): $V = x(16-2x)(10-2x)$ |
| Auxiliary equation (this comes from other information given in the problem): N/A | Graph (label axes and sketch a graph): | Main equation with only one variable: $V = x(16-2x)(10-2x)$ |
| Use the auxiliary equation to write your main equation with only two variables: $V = x(16-2x)(10-2x)$ | A suitable viewing window to see the min or max: [xmin, xmax] = [0, 5] [ymin, ymax] = [0, 150] | Answer to the original question: Max Volume: <u>144 in³</u> I should cut <u>2</u> inches from each corner. |
| Answer to the original question: I should cut <u>2</u> inches from each corner. | | Answer to the original question: I should cut <u>2</u> inches from each corner. |